COST Action TU1208 Civil Engineering Applications of Ground Penetrating Radar

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Structural evaluation of existing pavements based on deflection and GPR measurements

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Summary of the lecture (1/2)

Introduction to approaches for the evaluation of the structural properties of pavement

- Old-fashioned way: the equivalent single layer model
- Modern way: the back-calculation approach
- Multi-layer model of a road
- Application of loads and measurement of deflections

Evolution of mathematical models of pavement

- Pavement models based on the theory of elasticity
- Pavement models based on the strength of materials
- Model proposed by Burmister (1943)

Summary of the lecture (2/2)

Evaluation of the bearing capacity of a multilayered road structure

- The equivalent semi-infinite body
- Deflections and interpretation of the surface modulus
- Example: Back-calculation for a three-layer model of a road
- Sensitivity of the procedure

Application: Back-calculation and redesign of a road

- Measured deflections and present road structure
- Back-calculation and redesign with Qualidim
- Study of the influence of layer thicknesses on the road lifetime

Biography and contact details of the Author





Introduction to approaches for the evaluation of the structural properties of pavement



The old-fashioned way: equivalent single layer model

- Replace each layer of the multi-layer model of the road by one layer with "equivalent" thickness h_e (thicker than the sum of thicknesses h_i)
 - > Multi-layer model: thicknesses h_1 , h_2 , ...
 - The so-called 'equivalent factors' a1, a2, ... can be calculated by using the following formula:

$$a_i = \sqrt[3]{E_i / 500}$$

Here, E_i is the layer elasticity modulus, measured or taken from a table (this is a parameter depending on the layer material)

Thickness of the equivalent layer:

$$h_e = \sum a_i + h_i$$







Equivalent single layer model: thickness of overlay...

- Determine traffic (kN_c): Past, present and future traffic
- Graphs established in 1991 (BRRC report R56/85)





Traffic (kNc)

Thicknesses of crushed stone base course and asphalt layer



Traffic (kNc)



Equivalent single layer model: thickness of overlay...

- Traffic maps are used to determine the thicknesses H₁, H₂, H₃ of the ideal multi-layer road.
- The ideal equivalent thickness is: $H_e = \Sigma a_i \cdot H_i$ (for the equivalent 1-layer model).
- Then, do overlay: $W = (H_e h_e) / 2.7$ (with $a_i = 2.7$ for a bituminous layer) is the needed thickness of the bituminous overlay, in order to achieve equivalence with the ideal multi-layer road structure.



The modern way: back-calculation approach

- Objective: Determine E-modules of all layers
 - Compute deflection bowl from a multi-layer model
 - Compare the computed deflection bowl with the measured deflection bowl
 - If deflection bowls are not "identical" then modify E-modules and iterate...





The modern way: back-calculation approach

10 Iombre de 3	couches	Remark peut étr	er : 1 module e Taul Couche d'usure Sous-Couche 1 Sous-Couche 2	Nodule E of (R/mm²) E of on 1000 Г 50000 Г 400 Г	connu, Des chez ani (Ev) []	946 d' Kotropie MEN 1.00 1.00	0.35 0.50	Epainseur Innel 156 200 Adhérenc Gise patlat = 1.00 1.00
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Capteurs	sime)	pinn)	Déflesions(an)	Calcul	Capteurs	Déflexion	s calculées(µm)	Différences(am)
1	0	0	90	3033	1	44.9		0.07
2	300	0	80	534	2	39.9		0.12
3	600	0	70	350	3	35.5		-0.47
	900	0	60	200	4	29.7		0.29

- Then redesign the "current structure + overlay" (as if you are designing a new road) with a suitable software and estimate the expected lifetime.
- If results are poor, then do changes in deeper part of the road structure.

Back-calculation software tools

Free software:

"Qualidim": Intended for Belgium, to be used by non-specialists

- Commercial software:
 - Alizé-LCPC (itech-soft)
 - PAVERS (VIA Aperta)
 - Rosy (SWECO carlBro)
 - ELMOD (Dynatest)



Back-calculation: Qualidim





Model of the road: a multi-layer



Diameter: 2a **Pressure:** p For each layer i Thickness: h_i Modulus: E_i

Poisson: μ_i



Application of loads and their effects

• A load is applied to the multi-layer system...





Distribution of the load and measurement of deflections

 Only the part of the pavement that is subjected to stresses, will deform... (i.e. only the area inside the red cone, in the sketch)



The farther the deflection is measured from the centre of impact, the less the deflection is caused by the upper part of the road structure...





Evolution of mathematical models in pavement design

See also the book:

Frans Van Cauwelaert, « Pavement design and evaluation: The required mathematics and applications,» ISBN 978-2-960043-00-6



Pavement models based on the theory of elasticity

- Semi-infinite body subjected to a vertical load P
 - The subgrade is an isotropic body (Boussinesq, 1883)

$$\sigma_z = -\frac{3P}{2\pi z^2}$$

Definition of a stress concentration factor (Fröhlich, 1934)

$$\sigma_z = -\frac{\nu P}{2\pi z^2}$$
 Concentration: $\nu > 3$
Dispersion: $\nu < 3$

The subgrade is an orthotropic body (Lekhnitskii, 1963)

$$\sigma_{z} = -\frac{1+s+s^{2}}{s^{2}} \frac{P}{2\pi z^{2}} \qquad s^{2} = \frac{n-\mu^{2}}{n^{2}-\mu^{2}} \qquad n = \frac{E_{vert}}{E_{hor}}$$

Pavement models based on the theory of elasticity

Vertical stress vs anisotropy



(Lekhnitskii, 1963)



Pavement models based on the strength of materials

- Slab subjected to a vertical pressure p
 - Equilibrium equation

$$\left(\frac{\partial^2}{\partial r^2} + \frac{1}{r}\frac{\partial}{\partial r}\right)\left(\frac{\partial^2 w}{\partial r^2} + \frac{1}{r}\frac{\partial w}{\partial r}\right) = \frac{p-q}{D}$$
E, I
k, G
q

р

Westergaard (1924): The subgrade is a series of vertical springs (k)

$$q = kw$$

Pasternak (1954): The subgrade is a series of vertical (k) and horizontal springs (G)

$$q = -G\left(\frac{\partial^2 w}{\partial r^2} + \frac{1}{r}\frac{\partial w}{\partial r}\right) + kw$$

Pavement models based on the strength of materials

Surface deflection





Model proposed by Burmister (1943)

- Multilayered structure
 - Hypotheses of the theory of elasticity: equilibrium, continuity and elasticity for each layer

Model proposed by Burmister (1943)

 Mathematical solution (here, we skip the mathematical steps, but you are encouraged to calculate them!)

$$\left(\frac{\partial^2}{\partial r^2} + \frac{1}{r}\frac{\partial}{\partial r} + \frac{\partial^2}{\partial z^2}\right) \left(\frac{\partial^2 \varphi_i}{\partial r^2} + \frac{1}{r}\frac{\partial \varphi_i}{\partial r} + \frac{\partial^2 \varphi_i}{\partial z^2}\right) = 0$$

By introducing in the equation the expression $\phi(r,z) = J_0(mr)f(z)$, we obtain:

$$\left(\frac{\partial^2}{\partial r^2} + \frac{1}{r}\frac{\partial}{\partial r}\right) J_0(mr) = -m^2 J_0(mr)$$
$$J_0(mr) \left(m^4 - 2m^2\frac{\partial^2}{\partial z^2} + \frac{\partial^4}{\partial z^4}\right) f(z) = 0$$

$$\varphi_i(r,z) = J_0(mr) \left(A_i e^{mz} - B_i e^{-mz} + z C_i e^{mz} - z D_i e^{-mz} \right)$$

Model proposed by Burmister (1943)

 Stresses and displacements (again, we ignore the mathematical steps leading to these formulas):

$$\sigma_{z} = f(r) \left\{ Am^{2}e^{mz} + Bm^{2}e^{-mz} - (1 - 2\mu + mz)Cme^{mz} + (1 - 2\mu - mz)Dme^{-mz} \right\}$$

$$\tau_{rz} = f(r) \Big\{ Am^2 e^{mz} - Bm^2 e^{-mz} + (2\mu + mz)Cme^{mz} + (2\mu - mz)Dme^{-mz} \Big\}$$

$$u = \frac{f(r)}{E} \left\{ Am^2 e^{mz} + Bm^2 e^{-mz} + (1+mz)Cme^{mz} - (1-mz)Dme^{-mz} \right\}$$

$$w = \frac{f(r)}{E} \left\{ Am^2 e^{my} - Bm^2 e^{-my} - (2 - 4\mu - mz)Cme^{mz} - (2 - 4\mu + mz)Dme^{-mz} \right\}$$



Boundary conditions (Burmister)

- Surface (load)
 - Vertical stress = p
 - Shear stress = 0
- Interfaces (layers in contact)
 - Vertical stresses are all equal
 - Shear stresses are all equal
 - Deflections are all equal



- Displacements are equal: Friction
- Shear forces are null: Slip
- Intermediate scenario: Partial friction
- Subgrade, there are two alternatives
 - Semi-infinite body
 - Fixed bottom

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Evaluation of the bearing capacity of a multilayered road structure



The equivalent semi-infinite body





The further away from the centre of pressure...



 Deflection "at the centre of impact": is influenced by the whole road structure

 \rightarrow hence, the derived surface modulus characterizes the whole road structure

 Deflection "far away" from the centre of impact: it is influenced by the lower part of the road structure, only

 \rightarrow hence, the derived surface modulus characterizes the lower part of the road structure



Identical deflections





Interpreting the surface modulus

The surface modulus E₀(i) corresponds to the deflection w(i) measured at a distance r(i)

$$E_0(i) = \frac{2(1-\mu^2)}{r(i)w(i)} \frac{P}{2\pi} = pa^2 \frac{(1-\mu^2)}{r(i)w(i)}$$

- Pressure p, radius a, Poisson coefficient (Poisson's ratio) μ
- Model used: Boussinesq's theory, computation of the elastic modulus of a homogeneous half-space
- So, from the measured deflection w(i) at a distance r(i), we can compute the surface modulus E₀(i)



Example: Compute E₀, then draw conclusions on the E-moduli of the different layers of the 3-layer model

Input: Measured deflections at different distances from load centre



A three-layer road model with decreasing moduli

A three-layer road model with a stiff interlayer

A three-layer road model with a weak interlayer

A three-layer road model with an increasing modulus of the subgrade or a stiff bottom



Back-calculation of a three-layer (1/2)

- Let w₁, w₂, ... w_n be the deflections at the distances r₁, r₂, ..., r_n
- Let us assume the seed values E₁₀, E₂₀, E₃₀
- We compute the theoretical deflections z₀(1), z₀(2),..., z₀(n)
- We choose $E_{11} = E_{10} \cdot z_0(1) / w_0$, $E_{21} = E_{20} \cdot z_0(2) / w_1$, $E_{31} = E_{30} \cdot z_0(n) / w_n$
- With E₁₁, E₂₀, E₃₀, we compute z₁(1), z₁(2),... z₁(n)
- With E₁₀, E₂₁, E₃₀, we compute z₂(1), z₂(2),... z₂(n)
- With E₁₀, E₂₀, E₃₁, we compute z₃(1), z₃(2),... z₃(n)

Back-calculation of a three-layer (2/2)

- We apply the "Al Bush III" algorithm:
 - For k = 0 to 3, we define:

 $z_{k}(i) = a(i)\log E_{1.} + b(i)\log E_{2.} + c(i)\log E_{3.} + d(i)$

From this, we compute the solution for a(i), b(i), c(i), d(i)

We introduce these in the n equations (i=1,..,n):

 $z_0(i) = a(i)\log E_1 + b(i)\log E_2 + c(i)\log E_3 + d(i)$ We minimise $\sum_{1}^{n} \left[w(i) - z_0(i) \right]^2$ and obtain the expected values E_1 , E_2 , E_3

- If this sum of squares is "small enough" then we stop
 - Else we iterate with E_1 , E_2 , E_3 as new seed values...

Sensitivity of the procedure

- Given $E_1 = 10000$, $E_2 = 3000$, $E_3 = 500$
 - We compute w(0)=69.6, w(1)=38.1, w(2)=26.2, w(3)=19.1, w(4)=14.3, w(5)=11.2, w(6)=9.0, w(7)=7.5, w(8)=6.5

Backcalculation

w(0)	E ₁	E ₂	E ₃	Fit	Loops
69.6	10036	2993	500	0.02	7
75.0	6469	3351	503	0.06	6
58.0	33840	2371	497	0.10	7





Application: Back-calculation and redesign of a road



Deflections & present road structure

Deflections measured with a FWD in the middle of a concrete slab:





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Deflections & present road structure

Present road structure, hypothetical E-moduli (seed values):

Layer/Type of material	Thickness (mm)	Modulus (N/mm²)	Poisson Ratio
Concrete slabs (no dowels)	180	37000	0.20
Base course	500	2000	0.35
Stabilized subbase		350	0.50



Back-calculation

🍊 Terugbe	rekening								
Maximum a iteraties 10 Aantal lage 3	aantal :n	Opmerkir kan vast genomen	ng: 1 modulus worden Toplaag Onderlaag 1 Onderlaag 2	Modulus (N/mm²) 37000 2000 350	E bekend, vink aan	Graad van anisotropie (Ew/Eh) 1.00 1.00 1.00	Coëfficiënt van Poisson 0.20 0.35 0.50	Dikte (mm) 180 500	Totale hechting = 1; Volkomen 0.60 1.00
Deflectiemeter Geschatte elasticiteitsmoduli Curviameter Valgewicht 50 kN Geschatte elasticiteitsmoduli Straal (mm) Druk (N/mm²) v-co (mm) Deflectieresultaten 150.00 0.785 0 0									
150.00 0.785 0 0 Posities en gemeten deflecties Oppervlakte-e (N/mm²) Posities van de sensoren Sensorer (nm) Deflecties (um)				Intal iteraties 5 Criterium1 = 0 vereenstemming bereikt 2 = 2 gelijke elasticiteitsmoduli 3 = Geen overeenstemming 4 = Geschatte moduli Personen Berekende deflecties (um) Verschillen (um)			5 j bereikt eitsmoduli mming (µm)		
1	0	0	91	1941	⁹	91.2		-0.19	
2	300	0	76	581	2	75.6		0.37	_
3	600	0	59	374	3	58.9		0.11	_
4	900	0	46	320	4	46.2		-0.16	_
5	1200	0	36	307	5	36.9		-0.88	
6	1500	0	30	294	6	30.1		-0.07	
7	1800	0	26	283	7	25.0		0.98	
Berekening									



Back-calculation

Results (with software Qualidim©):

Layer/Type of material	Thickness (mm)	Modulus (N/mm²)	Poisson Ratio
Concrete slabs (no dowels)	180	35928	0.20
Base course	500	1081	0.35
Stabilized subbase		335	0.50

Present structure, hypothetical E-moduli (seed values):

Layer/Type of material	Thickness (mm)	Modulus (N/mm2)	Poisson Ratio
Concrete slabs (no dowels)	180	37000	0.20
Base course	500	2000	0.35
Stabilized subbase		350	0.50



Designing new roads...





🍊 Dimensio	onering - halfstijve	e of flexibele stru	ctuur				_ 🗆 ×
Structuur bev	waren S <u>t</u> ructuur ve	randeren <u>R</u> apport					
Verhardin	g				Verwacht a	antal zware voertu	igen 8.93E+006
Aantal lag	en (1 tot 4)		Aantal lage	-	-Schatting y	van de prestaties van	de totale structuur
		Туре	h (m	n)	1. Bezwijkk	ans (%) na	50.3
Astalt	AB-1B		<u> </u>	*	20 jaren		
Asfalt	AB-3A		▼ 100	-	2. Voor een	bezwijkkans van 50	%
	Complet	elv new	road		- Aantal j	imation of	traffic and
					- Aantal :	zware voertuigen	8.79E+006
	St	ucture			Hechting	expected I	lietime
(*)Gemodil		(**) Asfalt met g			Model	Standaardw	aarden 💌
Gebonder	n fundering						Details
• Туре		Schraal betor	n (R'bk = 10 MPa)	T			
O Modul	us (N/mm²)		450	-			
h (mm	J		150	*			
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	dering II				Perek		amina Tama
• Туре		Type I		-	Derek		orming v rerug
O Modul	lus (N/mm²)						
h (mm)		400	*			
Ondergro	nd						
С Туре							
⊙ C.B.R.		4					
O Modul	us (N/mm²)						
Graad	l van anisotropie		1.00				



Overlay on existing road...





🝊 Versterking - Overlay op besta	and beton				<u> </u>
Overlay op bestaar Verharding Aantal lagen (1 tot 4)	ad beton	ıtal lagen	Verwacht aa	Soorten van versterking Overlay ntal zware voertuigen	C Inlay 8.93E+006
(**) Asfalt Modulus (N/ Beton 35928	Type	h (mm) 50 + 180 +	Schatting va Bezwijkkar 20 jaren ESTI Voor een t Aant (2) Aantal zw	n de nrestaties van de total ns (%) na mate of traffic rezematies van de traffic rected life-ti vare voertuigen	0.0 c and meo 8.69E+009
(*)Gemodificeerd bitumen (**) Gebonden fundering C Type Existing C Modulus (N/mm²) h (mBack-calcul Ongebonden fundering C Type C Type C Modulus (N/mm²) 1 h (mm)	Asfalt met gekende n structure, ated E-mod	adulus	Model Periode (tijd) Voorschrifter Type van ove in de voegen I✓ Temper Gekozen ter DGB / I = 3	Standaardwaarden 0-10 jaar erdracht Ongedeuvelde var ratuurgradiënt (In-reken mperatuurgradiëntenmodel : 1,50 m	Details Details Details Details
Onderfundering ○ Type ⓒ Modulus (N/mm²) 1 h (mm) Ondergrond ○ Type ○ C.B.R. ⓒ Modulus (N/mm²) 3	081 💌	250	Bereke	ning 🖾 Spoorvorming	√ Terug
Modulus (N/mm ²) Graad van anisotropie	50 💌	1			



Evaluation with a theoretical model

• Concept: Theoretical structure:

Layer/Type of material	Thickness (mm)	Modulus (N/mm2)	Poisson Ratio
Concrete slabs (no dowels)	Between 180 and 200	37661	0.20
Unbound base course, granular material Type I	400	650	0.45
subbase (stabilized with chalk)	200	2000	0.50
Clay ground		20	0.50

Traffic: 100 trucks/day, 300 days/year, growth +2% per year:

Axle load:	50 kN	90 kN	120 kN	
100 trucks per day,	20%	60%	20%	
300 days per year				



Study of the influence of thickness on the road lifetime...

Cimensionnement des chaussées - S.P.W.
DIMENSIONNEMENT
7 Dimensionnement des chaussées - 5 P.W Cas - Dim 1
Geval Taal Database Functionaliteiten Verkeer Klimaat Berekening Hulp Informatie
 ✓ Functionaliteit: Dimensionering ✓ Verkeer: WIM ✓ Klimaat: Namur ✓ Structuur: Halfstijf Terugbereke
Versie 2.3.26.0 20.11.2012
DimMET Conter
Version 2.3.26.0



Study of the influence of thickness on the road lifetime...





2 cm extra thickness is important!

 Lowering the thickness of the concrete slab in the theoretical model makes the estimated lifetime drop drastically

Thickness of concrete slab (mm)	200	190	180
Number of standard axles N _c that can go over the road	2.45 *10 ⁶	6.60*10 ⁵	1.52*10 ⁵
Estimated life-time (in years)	> 40	18	5

Note: this does not mean that the thicknesses of the layers underneath are of no significance...



Author

Dr. Carl Van Geem (c.vangeem@brrc.be) is a researcher in road management and monitoring techniques, since 2004 he is working in the Mobility, security and road management (MSM) division of the Belgian Road Research Centre (BRRC), in Brussels, Belgium. He is a Working Group Member of the COST Action TU1208.

In 1996, Carl Van Geem earned the doctoral degree in technical sciences from the Research Institute on Symbolic Computation (RISC-Linz), Johannes Kepler University, Linz, Austria.



The BRRC has several devices for the evaluation of road surface properties (roughness, skid resistence), for pavement management (visual inspection device "SAND"), and for measuring the bearing capacity of roads (FWD, curviameter, GPR). The main topic of Carl's research is the interpretation of data obtained with these monitoring devices for an optimal management of road maintenance. Carl participated in several national and international research projects, including a "national pre-normative research project on the indicators of roughness", the COST Action 354 "Performance Indicators for Road Pavements", the PIARC technical committee D1 "Management of Road Infrastructure Assets", and the FP7 project "Tomorrow's Road Infrastructure Monitoring and Management (TRIMM)".





Thank you

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